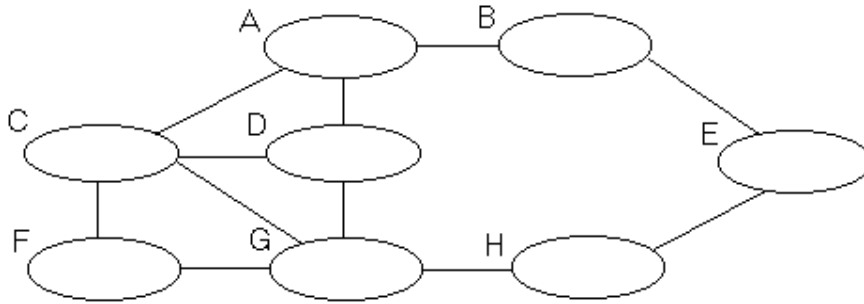


TRIGONOMETRY | STUDENT WORK | PROFICIENCIES

Logic puzzle



Part 1: Solve the puzzle.

(Place the people in the correct houses)

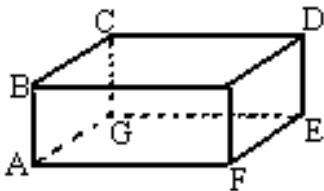
Part 2: Prove that your solution is the only solution—that no other solution works.

Use the reference sentences 1-10 in the body of your proof or as footnotes. The proof steps should be in good order.

- 1) 8 students live in the houses A B C D E F G H. Some are connected by phone lines (direct lines between the oval houses).
- 2) The 4-letter name people are not connected to each other.
- 3) Vera is not connected to Gabriel.
- 4) The 7-letter name people are not connected to each other.
- 5) Venus has EXACTLY two connections.
- 6) Paul is not connected to Tanisha.
- 7) The 5-letter name people are not connected to each other.
- 8) Nija is not in F.
- 9) The V-names are not connected.
- 10) Sean is not connected to Maria.


Proficiency problem

You wish to find the volume of a building. The base is a parallelogram and the sides are vertical. The roof is also a parallelogram parallel to the base.



You may not climb the building nor throw anything on it or at it.

You have with you:

a yardstick
 tent pegs
 tuna sandwiches
 a scientific calculator
 a backpack
 a roll of electric tape
 scissors
 a sextant 
 a machete
 a level

graph paper and colored pencils
 a camera (Polaroid) and film
 trig tables
 an axe
 a thermos of tea
 a hammer
 a box of straws
 a flashlight with batteries
 2 compasses (1 of each kind)
 a ball of twine

Find the volume efficiently (minimize time and energy).

- Draw appropriate pictures and label everything.
- State the formulas to be used and show how to solve them.
- Show what you will measure and how.

06/16

1) First I will find the area of the base.
To do that, I will measure the angle $\angle GAF$ with the sextant.



To measure $\angle GAF$ I will align the sextant with segment AF. (i.e. 90° ^{in front of} \perp ^{horizontal} parallel AF) just behind the wall

Looking through the straw I will determine the angle. After that, I will measure with my yard stick segments AG and AF.

Once I have those measures I will put them in the equation: $\text{Area} = \frac{1}{2} b h$. It would look like this.

$$A = \frac{1}{2} b h \rightarrow (\text{distance of } AF) \rightarrow (\sin \theta) (\text{distance of } AG)$$

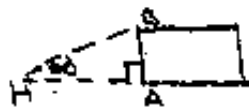
The result is the area of the base parallelogram AFE G.

2) I will determine the height of the building.

First I will stand next to corner A and measure a line that extends from AF.

Where The end of that line is H.

From H, I will use my sextant to determine the $\angle BHA$.

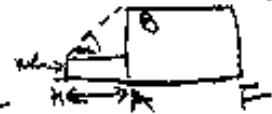


06/16

The sextant \odot must be vertical and parallel to HA . Once I have looked through the straw and determined the angle I will put the #'s in the following formula:

(Height of building) (distance of survey line)

$$BA = HA \tan \alpha + \text{my height}$$



3) Once I ^{know} both the height of the building and the area of the base, I will multiply them in order to attain the volume.

$$V = A H \rightarrow \left(\begin{array}{l} \text{(distance } HA \text{ times } \tan \alpha) \\ \text{plus my height} \end{array} \right)$$

↓
(distance A times)
(distance AB sin α)

notes

1. Vera - 4 letters
2. Venus - 5
3. Gabriel - 7
4. Paul - 4
5. Tanisha - 7
6. Nija - 4
7. Sean - 4
8. Maria - 5

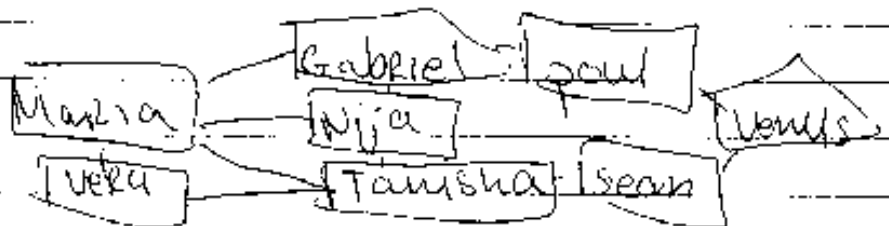
Vera, Paul, Nija, Sean were not connected

Gabriel, Tanisha are not connected

Venus maria are not connected

Sean is not connected to maria

Nija is not in "7"



Pg. 1

If the four-letter names are not connected to each other then the only space they can be placed without being connected is F, D, H, and B.

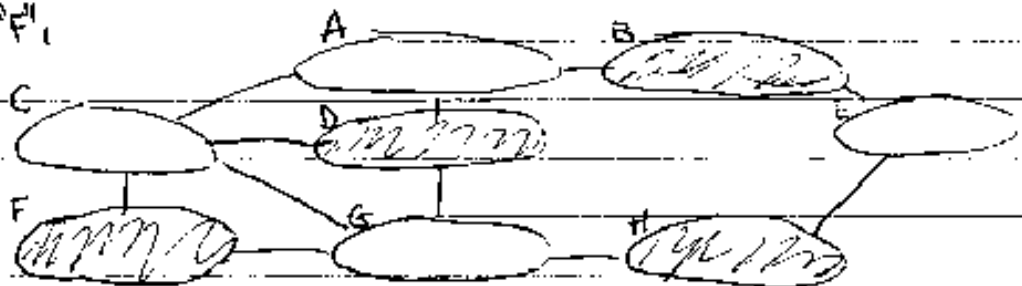
If you put a four letter name in "C" you would have to place the other three four-letter names in B, H, and G, because C is connected to F, A, D, and G. Which is leaving three names and three houses. That won't work because the three houses are connected.

If you put a four letter name in "E" it would leave three spaces too because "E" is connected to F, C, D, H, which leaves you A, B, G. As you can see those are connected too so that doesn't work.

But if you place a four-letter word in "F" that leaves A, D, H, B, G. Because they are not connected ~~and~~ C, and G are connected so there are no four-letter names in C or G. Now if you place a four-letter

Pg. 2

name in "A" that means you can't place no four letter names in D, or B which leave two names, and two places H, and E. That wouldn't work because the two four letter names ~~are~~ would be connected. So no four letter name ~~can~~ can be placed in "A". So now we have limited our houses down to ^{five} ~~four~~ F, D, H, B, E. Now E is connected to B, and H which means the four letter names would end up being connected. So no four letter names can be placed in "E". Which leaves three ~~two~~ four letter names, and three space. Tell what do you know they are not connected D, B, H aren't connected to each other and aren't connected to "F".



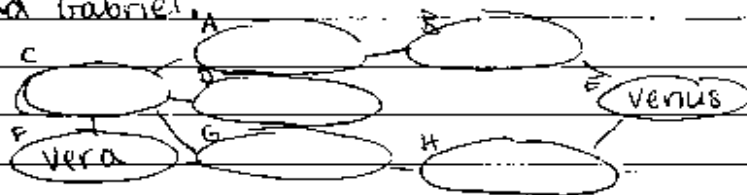
F, D, H, B

The people with seven letters in their names were not connected neither were the people with five letters in their names. So it's 2 people with seven

Pg. 3

letters in their name Tamisha, and Gabriel.
And there are two people with five letters
in their names. The ^(Venus, Maria) spots that are left
open are C, A, G, E. Now I have to set it
up in a way the seven letter names don't
connect, and the five letter names don't connect. *

Since the V-letter names don't connect
there ~~is~~ ^{is} ~~but so many~~ place only one
place ~~that~~ ^{where Venus} can go without being
connected to ~~her~~ ~~that is in E~~ now
Vera can't be placed in B, or H, so that
leaves her D, and F. Now "D" is connected
to A, G, and C. Since Vera is not connected
to Gabriel she has to be placed in the
"F" spot because out of A, G, and C
Gabriel has to be placed and he would
have ended up connecting with Vera. So
now Vera is disconnected from Venus,
and Gabriel.



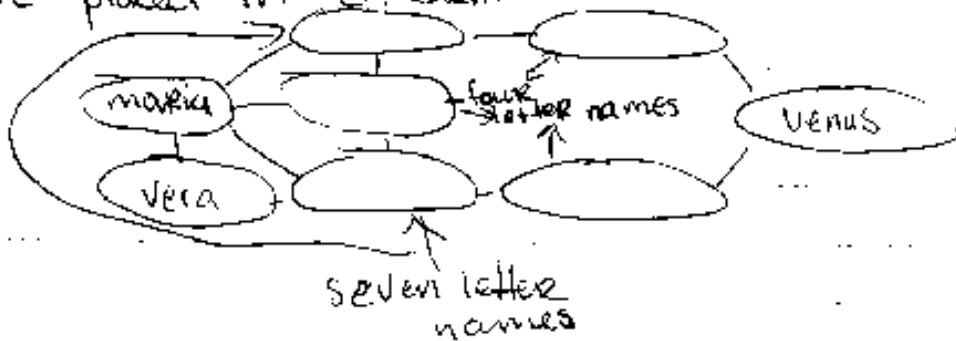
If the five letter names can't connect
that means maria has to be placed
in "C". Because if you place her in



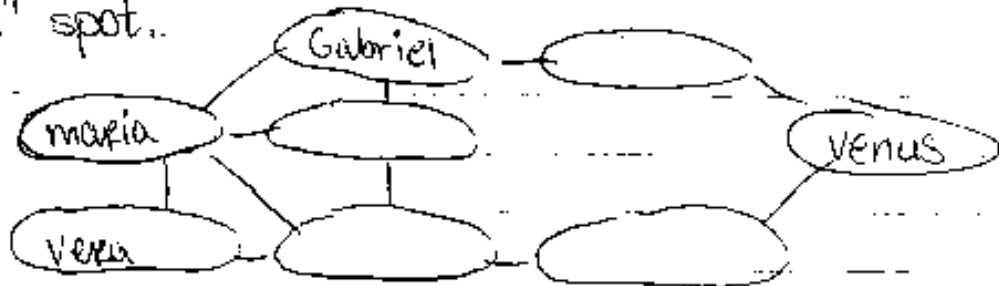
and have exactly two connections
that is E. Because "A" has three
connections (C, D, B). "G" has ~~three~~ ^{four} connections
(C, F, D, H) "C" has ~~three~~ ^{four} connections (F, G, D, A)
F, D, B, H are only for four letter names.
• And "E" is the only house ^{left} with exactly
two connections.

Fig 4

if you put her in "G" the seven-letter names will connect. So since ~~A, B, H~~ ~~are taken up by four-letter names~~ ~~are taken up by Venus~~ there are only three spots, A, C, G. And Maria can't be placed in A, or G, she has to be placed in "C". (that would work)

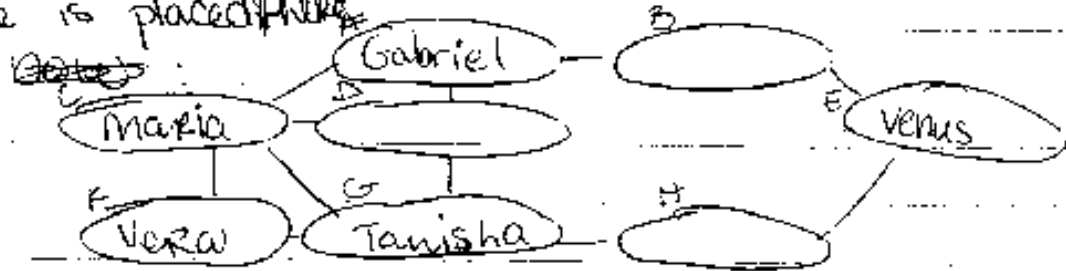


Since Gabriel wasn't connected to vera he had to be placed in the "A" spot. Because there are only two spots left "A", and "G". "G" is connected to vera so Gabriel has to be placed in the "A" spot.



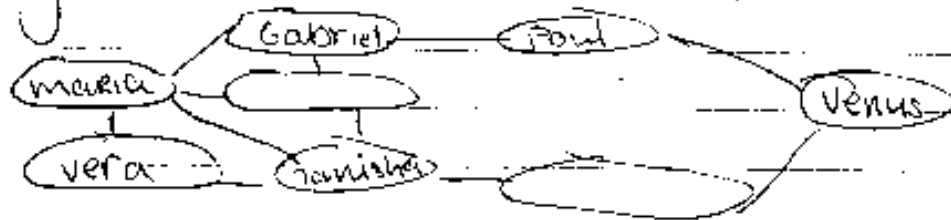
~~Now~~ Now there is only one spot left which leaves "G". Since Tanisha

is the only one left that where she is placed ~~here~~



Now I have to fill in the four letter names.

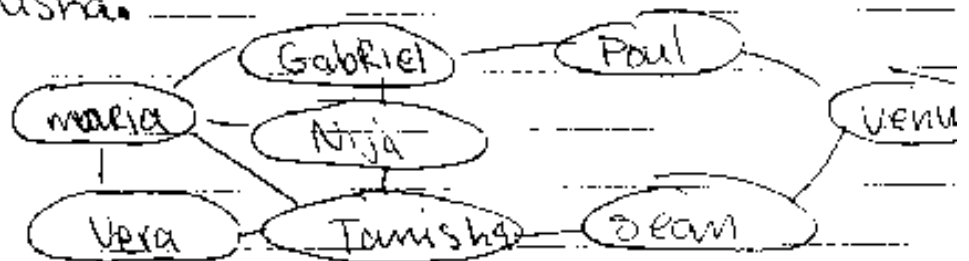
If Paul is not connected to Tanisha he has to be placed in the "B" spot because, if you place him in either "D", or "H" it will connect to a "G" where Tanisha is placed. So the only place Paul can be placed without being connected to Tanisha is "B".



The last two people who names need to be filled in are Nija and Sean. Now we already know Nija can't be in the "F" spot. For one, she wasn't allowed that spot in the first place and for two it's already taken. And Sean isn't.

Pg. 6

connected to maria so he had to be placed in "H" because, if you place him in "D" it is connected to "C" where maria was placed at so in order for sean to be disconnected from maria, he would have to be placed in the "H" spot, which put Nija in the "D" spot because she was the only one ~~was~~ out of the four letter named people who was left and the only person who could be connected to Maria, Gabriel, and Tanisha.



None of the 4-letter named people are connected
Vera, and Gabriel aren't connected.

None of the 7-letter name people were connected

Venus had exactly two connections

Paul is not connected to Tanisha

The five letter name people weren't connected

Nija wasn't in "F"

The 6-names are not connected

Sean is not connected to Vera